



Cambridge International AS & A Level

MATHEMATICS

9709/01

Paper 1 Pure Mathematics 1

For examination from 2020

MARK SCHEME

Maximum Mark: 75

Specimen

This document has **10** pages. Blank pages are indicated.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1: Marks must be awarded in line with: - the specific content of the mark scheme or the generic level descriptors for the question - the specific skills defined in the mark scheme or in the generic level descriptors for the question - the standard of response required by a candidate as exemplified by the standardisation scripts.
GENERIC MARKING PRINCIPLE 2: Marks awarded are always whole marks (not half marks, or other fractions).
GENERIC MARKING PRINCIPLE 3: Marks must be awarded positively: - marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate - marks are awarded when candidates clearly demonstrate what they know and can do - marks are not deducted for errors - marks are not deducted for omissions - answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.
GENERIC MARKING PRINCIPLE 4: Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.
GENERIC MARKING PRINCIPLE 5: Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mark Scheme Notes

Marks are of the following three types.

- M** Method mark, given for a valid method applied to the problem. Method marks can still be given even if there are numerical errors, algebraic slips or errors in units. However the method must be applied to the specific problem, e.g. by substituting the relevant quantities into a formula. Correct use of a formula without the formula being quoted earns the M mark and in some cases an M mark can be implied from a correct answer.
- A** Accuracy mark, given for an accurate answer or accurate intermediate step following a correct method. Accuracy marks cannot be given unless the relevant method mark has also been given.
- B** Mark for a correct statement or step.
- DM or DB** M marks and B marks are generally independent of each other. The notation DM or DB means a particular M or B mark is dependent on an earlier M or B mark (indicated by *). When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT below).
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures (sf) or would be correct to 3 sf if rounded (1 decimal point (dp) for angles in degrees). As stated above, an A or B mark is not given if a correct numerical answer is obtained from incorrect working.
- Common alternative solutions are shown in the Answer column as: '**EITHER** Solution 1 **OR** Solution 2 **OR** Solution 3 ...'. Round brackets appear in the Partial Marks column around the marks for each alternative solution.
- Square brackets [] around text show extra information not needed for the mark to be awarded.
- The total number of marks available for each question is shown at the bottom of the Marks column in bold type.

The following abbreviations may be used in a mark scheme.

- AG** Answer given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid).
- CAO** Correct answer only (emphasising that no 'follow through' from an error is allowed).
- CWO** Correct working only
- FT** Follow through after error (see Mark Scheme Notes for further details).
- ISW** Ignore subsequent working
- OE** Or equivalent form
- SC** Special case
- SOI** Seen or implied

Question	Answer	Marks	Partial Marks	Guidance
1(a)	Gradient of $CE = 2.5$	1	B1	
	Gradient of $DE = 2.1$	1	B1	
		2		
1(b)	$f'(2) = 2$	1	B1	Accept reasonable conclusion following <i>their</i> gradient

Question	Answer	Marks	Partial Marks	Guidance
2	$f^{-1}(x) = \frac{x-2}{3}$	1	B1	
	$gf(x) = 4(3x + 2) - 12$	1	B1	
	Equate $f^{-1}(x)$ and $gf(x)$ expressions, $x = \frac{2}{7}$	2	M1A1	
		4		

Question	Answer	Marks	Partial Marks	Guidance
3	$7 + (n - 1)d = 84$ and/or $7 + (3n - 1)d = 245$	1	B1	
	$(n - 1)d = 77$, $(3n - 1)d = 238$ SOI OR $2nd = 161$ explicitly stated	1	B1	
	$\frac{n-1}{3n-1} = \frac{77}{238}$	1	M1	(must be from the correct u_n formula) OR other attempt to eliminate d e.g. substitute $d = \frac{161}{2n}$. (If n is eliminated d must be found)
	$n = 23$ ($d = \frac{77}{22} = 3.5$)	1	A1	
		4		

Question	Answer	Marks	Partial Marks	Guidance
4	Attempt integration	1	M1	
	$f(x) = 2(x+6)^{\frac{1}{2}} - \frac{6}{x} (+c)$	2	A1A1	Accept unsimplified terms, A1 for each term
	$2(3) - \frac{6}{3} + c = 1$	1	M1	Substitute $x = 3$, $y = 1$. c must be present
	$[c = -3]$ $f(x) = 2(x+6)^{\frac{1}{2}} - \frac{6}{x} - 3$	1	A1	
		5		

Question	Answer	Marks	Partial Marks	Guidance
5(a)	$y = (x-2)^2 + 3(x-2) + 4 = x^2 - x + 2$	2	M1A1	
5(b)	Reflection [in] y axis	1	B1	In either order
	Stretch factor 3 in y direction	2	B1B1	B1 for stretch, B1 for factor 3 in y direction
		3		

Question	Answer	Marks	Partial Marks	Guidance
6(a)	Coefficient of x^2 is 240	1	B1	
	Coefficient of x^3 is $20 \times 8 \times (-1) = -160$	2	B2	B1 for +160
		3		
6(b)	Product needs exactly 2 terms	1	M1	$3 \times$ their 240 + their -160
	$720 - 160 = 560$	1	A1FT	FT for candidate's answers
		2		

Question	Answer	Marks	Partial Marks	Guidance
7(a)	Replace $\tan x$ by $\frac{\sin x}{\cos x}$ $1 + \frac{\sin x^2}{\cos x} = 5 \cos x$	1	M1	Correct formula
	Replace $\sin x^2$ by $1 - \cos x^2$	1	M1	Correct formula used in appropriate place
	$6 \cos x^2 - \cos x - 1 (=0)$	1	A1	AG
		3		
7(b)	Solution of quadratic $\left[c = -\frac{1}{3} \text{ or } \frac{1}{2}\right]$	1	M1	Correct method seen
	$x = 60^\circ \text{ or } 109.5^\circ$	2	A1A1	
		3		

Question	Answer	Marks	Partial Marks	Guidance
8(a)	$-12(3 - 2x)^{-2} \times -2$	2	B1B1	B1 for $-12(3 - 2x)^{-2}$, B1 for -2
8(b)	$\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt} = 0.4 \div 0.15$	1	M1	OE; chain rule used correctly
	$\frac{24}{(3 - 2x)^2} = \frac{8}{3}$	1	M1	Equates their $\frac{dy}{dx}$ with their $\frac{8}{3}$ or $\frac{3}{8}$ and method seen for solution of quadratic equation
	$x = 0 \text{ or } 3$	2	A1A1	
		4		

Question	Answer	Marks	Partial Marks	Guidance
9(a)	$BC^2 = r^2 + r^2 = 2r^2 \rightarrow BC = r\sqrt{2}$	1	B1	AG
9(b)	Area sector $BCFD = \frac{1}{4}\pi(r\sqrt{2})^2$ seen or implied	1	M1	Expect $\frac{1}{2}\pi r^2$. (F is intersection of large circle with AE)
	Area $\triangle BCD = \frac{1}{2}(2r)r$	1	M1*	Expect r^2 (could be embedded)
	Area segment $CFDA = \frac{1}{2}\pi r^2 - r^2$	1	A1	OE
	Area semi circle $CADE = \frac{1}{2}\pi r^2$	1	B1	
	Shaded area $= \frac{1}{2}\pi r^2 - (\frac{1}{2}\pi r^2 - r^2)$ OR $\pi r^2 - \left[\frac{1}{2}\pi r^2 + \left(\frac{1}{2}\pi r^2 - r^2 \right) \right]$ $= r^2$	1	DM1	Depends on the area $\triangle BCD$
		1	A1	
		6		

Question	Answer	Marks	Partial Marks	Guidance
10(a)	$(-2, 1)$	1	B1	
10(b)	Gradient of $CD = \frac{1}{2} \div 3\frac{1}{2} = \frac{1}{7}$	1	B1	
	Gradient of $AB = -7$	1	M1	With gradient $-1/\text{their } m$
	Equation of AB is $y - 1\frac{1}{2} = -7(x - 1\frac{1}{2})$	1	M1	
	$y = -7x + 12$	1	A1	
		4		
10(c)	$x^2 + (12 - 7x)^2 + 4x - 2(12 - 7x) - 20 (= 0)$	1	M1	Substituting their AB equation into circle equation
	$(50)(x^2 - 3x + 2) (= 0)$	1	A1	
	$x = 1, 2$	1	A1	Dependent on method seen for solving quadratic equation
		3		

Question	Answer	Marks	Partial Marks	Guidance
11(a)	$x^2 + 6x - 8 = (x + 3)^2 - 17$ OR $2x + 6 = 0 \rightarrow x = -3 \rightarrow y = -17$	2	B1B1	B1 for $(x + 3)^2$, B1 for -17 OR B1 for $x = -3$, B1 for $y = -17$
	Range $f(x) \geq -17$	1	B1FT	FT; following through visible method
		3		
11(b)	$(x - k)(x + 2k) = 0 \equiv x^2 + 5x + b = 0$	1	M1	Realises the link between roots and the equation
	$k = 5$	1	A1	Comparing coefficients of x
	$b = -2k^2 = -50$	1	A1	
		3		
11(c)	$(x + a)^2 + a(x + a) + b = a$	1	M1*	Replaces 'x' by 'x + a' in 2 terms
	Uses $b^2 - 4ac$, $9a^2 - 4(2a^2 + b - a)$	1	DM1	Any use of discriminant
	$a^2 < 4(b - a)$	1	A1	AG
		3		

Question	Answer	Marks	Partial Marks	Guidance
12(a)	$a = 2$	1	B1	
12(b)	$y = x^3 - 4x^2 + 4x$	1	B1	
	$\frac{dy}{dx} = 3x^2 - 8x + 4$	2	B2FT	FT B1 for $3x^2$, B1 for $-8x + 4$
	$(x - 2)(3x - 2) = 0 \rightarrow b = \frac{2}{3}$	1	B1	Dependent on method seen for solving quadratic equation
		4		
12(c)	Area = $\int y \, dx = \left[\frac{x^4}{4} - \frac{4x^3}{3} + 2x^2 \right]$	2	B2	B1 for $\frac{x^4}{4}$, B1 for $\frac{4x^3}{3} + 2x^2$
	$4 - \frac{32}{3} + 8$	1	M1	Apply limits $0 \rightarrow 2$
	$\frac{4}{3}$	1	A1	Unsupported answer receives 0 marks
		4		
12(d)	$\frac{d^2y}{dx^2} = 6x - 8 = 0, x = \frac{4}{3}$	2	M1* A1	Attempt 2nd derivative and set = 0
	When $x = \frac{4}{3}$, $\frac{dy}{dx}$ (or m) = $-\frac{4}{3}$	2	DM1A1	
		4		